

FIRST SEMESTER DIPLOMA EXAMINATION IN ENGINEERING/  
TECHNOLOGY—OCTOBER, 2010

TECHNICAL MATHEMATICS-I  
(Common-Except DCP and CABM)

[Time : 3 hours

(Maximum marks : 100)

PART—A

(Answer all questions. Each question carries 2 marks.)

Marks

- I (a) Find the values of a, b, c and d, given that :

$$\begin{bmatrix} 2a & a + 3b \\ 5-c & d \end{bmatrix} = \begin{bmatrix} 4 & 11 \\ 7 & 0 \end{bmatrix}$$

(b) Evaluate  $\begin{vmatrix} \sin \theta & \cos \theta \\ -\cos \theta & \sin \theta \end{vmatrix}$

- (c) If  ${}^n C_{12} = {}^n C_{13}$ , what is the value of n?

- (d) Prove that  $\tan A + \cot A = 2 \operatorname{cosec} 2A$ .

- (e) Find the angle of inclination of the line joining the points (5, 3) and (-8, 3).

(5×2=10)

PART—B

(Answer any five questions. Each question carries 6 marks.)

II (a) If  $A = \begin{bmatrix} 2 & 3 & 4 \\ 1 & 2 & 3 \\ -1 & 1 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & 3 & 0 \\ -1 & 2 & 1 \\ 0 & 0 & 2 \end{bmatrix}$ , find

AB and BA and show that  $AB \neq BA$ .

- (b) Solve the following equations using Cramer's rule :

$$2x + 3y - z = 5$$

$$x - 2y + 3z = 6$$

$$3x - y + 2z = 7.$$

- (c) Obtain the coefficient of  $x^{12}$  in the expansion of  $\left(x^2 - \frac{1}{x^2}\right)^{10}$

- (d) Prove that  $\sin^2 A - \cos^2 A = 2 \sin^2 A - 1 = 1 - 2 \cos^2 A$ .
- (e) If  $\sin A = \frac{4}{5}$  and  $\sin B = \frac{12}{13}$ ,  $A$  and  $B$  are acute angles, find  $\cos(A - B)$ .
- (f) Prove that  $\sin(A + B) \sin(A - B) = \sin^2 A - \sin^2 B$ .
- (g) Express the equation  $3x + 4y - 12 = 0$  in (i) Slope-intercept form and (ii) intercept form. Hence find the slope and the intercepts made on the axes.

(5×6=30)

## PART—C

(Answer four full questions. Each question carries 15 marks.)

III (a) If  $A = \begin{bmatrix} 2 & 0 & 1 \\ 2 & 1 & 3 \\ 1 & -1 & 0 \end{bmatrix}$ , find  $A^2 - 3A + 5I$ .

4

(b) Express the matrix  $\begin{bmatrix} 1 & 0 & 5 \\ -2 & 1 & 6 \\ 3 & 2 & 7 \end{bmatrix}$  as the sum of a symmetric and skew-symmetric matrices.

4

(c) Solve the following system of equations using the inverse of the coefficient matrix :

$$\begin{aligned} 3x - 2y + 3z &= 4 \\ 2x + y - z &= 2 \\ 4x - 3y + 2z &= 3. \end{aligned}$$

7

OR

IV (a) If  $A = \begin{bmatrix} 2 & 3 \\ 0 & 1 \end{bmatrix}$  and  $B = \begin{bmatrix} 3 & 4 \\ 2 & 1 \end{bmatrix}$ , verify that  $(A + B)^T = A^T + B^T$ .

5

(b) Solve for  $x$  if  $\begin{vmatrix} 1 & 2 & 3 \\ 2 & x & 4 \\ 3 & 4 & 5 \end{vmatrix} = 0$ .

3

(c) If  $P = \begin{bmatrix} 1 & 2 \\ 4 & 9 \end{bmatrix}$  and  $Q = \begin{bmatrix} 4 & 1 \\ 6 & 5 \end{bmatrix}$ , verify that  $(PQ)^{-1} = Q^{-1} P^{-1}$ .

7

V (a) Find the middle terms in the expansion of  $\left(x^2 + \frac{2}{x}\right)^7$

6

(b) Expand  $(3x + 2y)^5$ .

4

(c) Show that  $\sin 60^\circ \cos 30^\circ - \cos 60^\circ \sin 30^\circ = \frac{1}{2}$ .

5

OR

Marks

- VI (a) Find the constant term in the expansion of  $\left(x^3 + \frac{3}{x^2}\right)^{15}$ . 5  
 (b) Evaluate  $\tan^2 60^\circ + 3 \tan^2 45^\circ$ . 4  
 (c) If  $\sin \theta = -\frac{4}{5}$ ,  $\theta$  is in the 3rd quadrant, find all other trigonometric functions of  $\theta$ . 6
- VII (a) Prove that  $\sin \theta + \sin 3\theta + \sin 5\theta + \sin 7\theta = 4 \cos \theta \cos 2\theta \sin 4\theta$ . 6  
 (b) Prove that  $2 \tan 10^\circ + \tan 40^\circ = \tan 50^\circ$ . 5  
 (c) In any triangle ABC, prove that  $a^2 + bc = b^2 + c^2$ , if  $A = 60^\circ$ . 4
- OR
- VIII (a) Prove that  $\cos 20^\circ \cos 40^\circ \cos 80^\circ = \frac{1}{8}$ . 5  
 (b) If  $A + B = 45^\circ$ , show that  $(1 + \tan A)(1 + \tan B) = 2$ . 4  
 (c) State and prove Sine rule. 6
- IX (a) Solve the triangle with  $a = 2$  cm,  $b = 3$  cm and  $c = 4$  cm. 5  
 (b) Find the acute angle between the lines  $2x - y + 3 = 0$  and  $3x - 3y + 4 = 0$ . 5  
 (c) If A (1, -1), B (-2, 1) and C (3, 5) are the vertices of a triangle, then find the equation of the median through B. 5
- OR
- X (a) Using Napier's formula, find the values of the angles A and B in  $\Delta ABC$ , if  $a = 5$  cm,  $b = 8$  cm and  $C = 30^\circ$ . 5  
 (b) Find the angles of the triangle having vertices (3, 2), (5, -4) and (1, -2). 5  
 (c) Show that the three lines are concurrent :  
 $5x + 2y - 4 = 0$   
 $2x + 5y + 11 = 0$  and  
 $3x - 4y - 18 = 0$ . 5
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